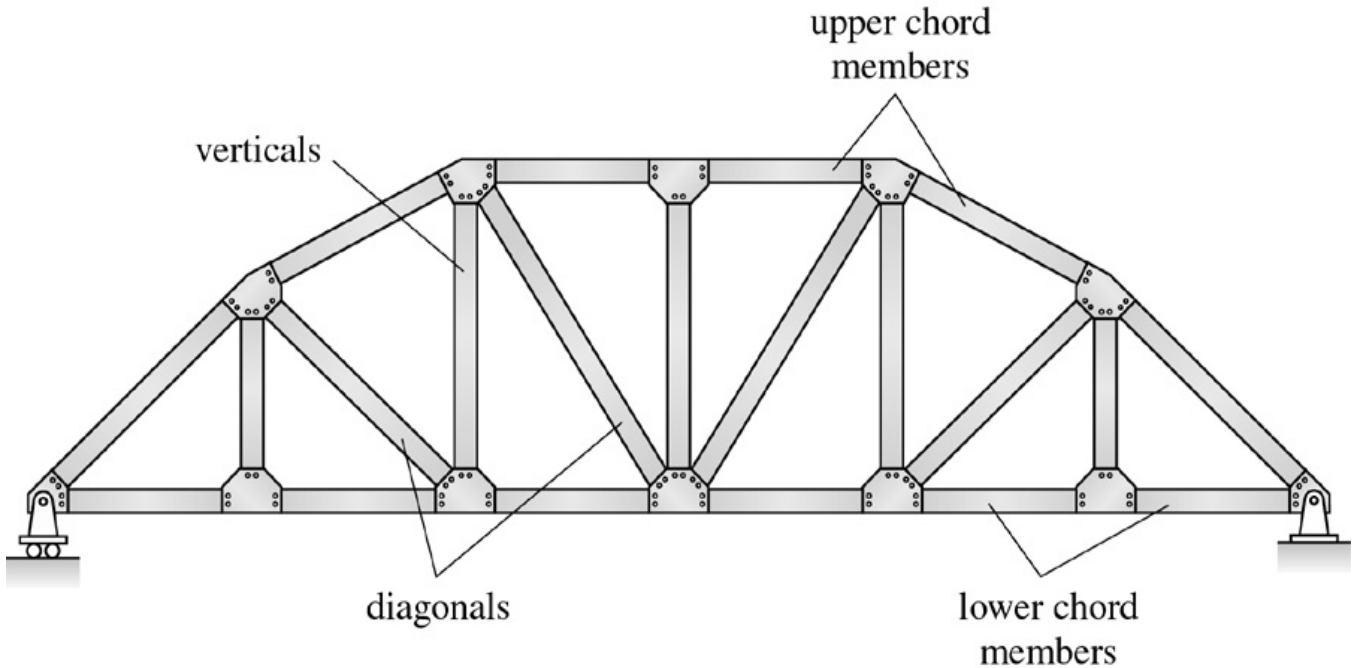
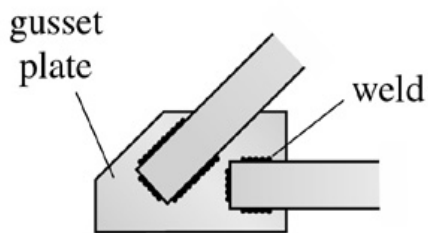


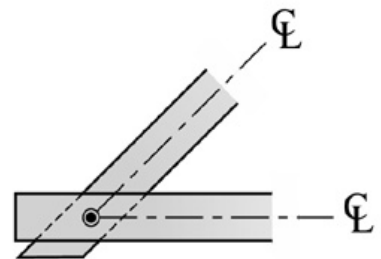
Truss Structures



(a)

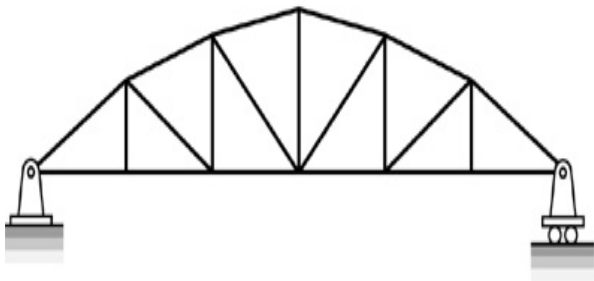
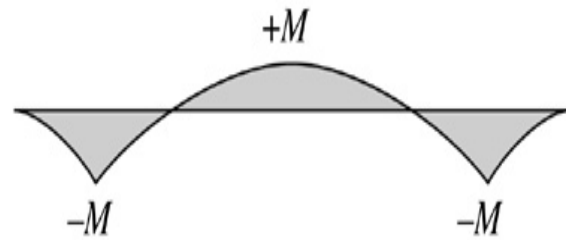
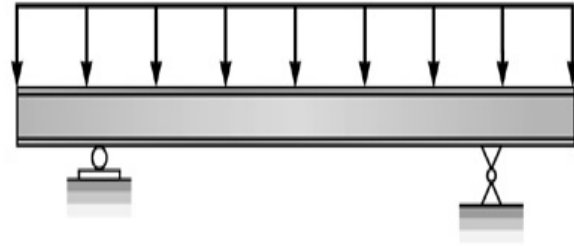
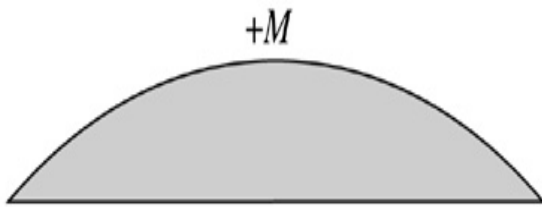
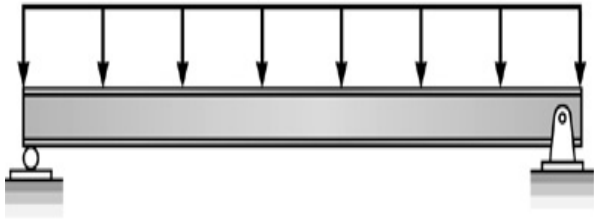


(b)

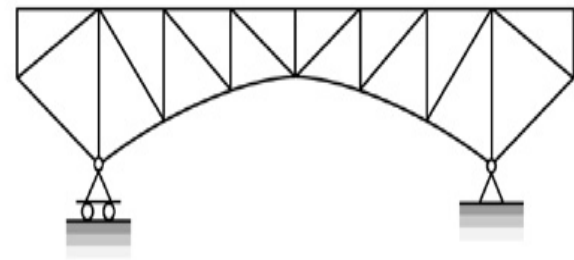


(c)

Truss Definitions and Details

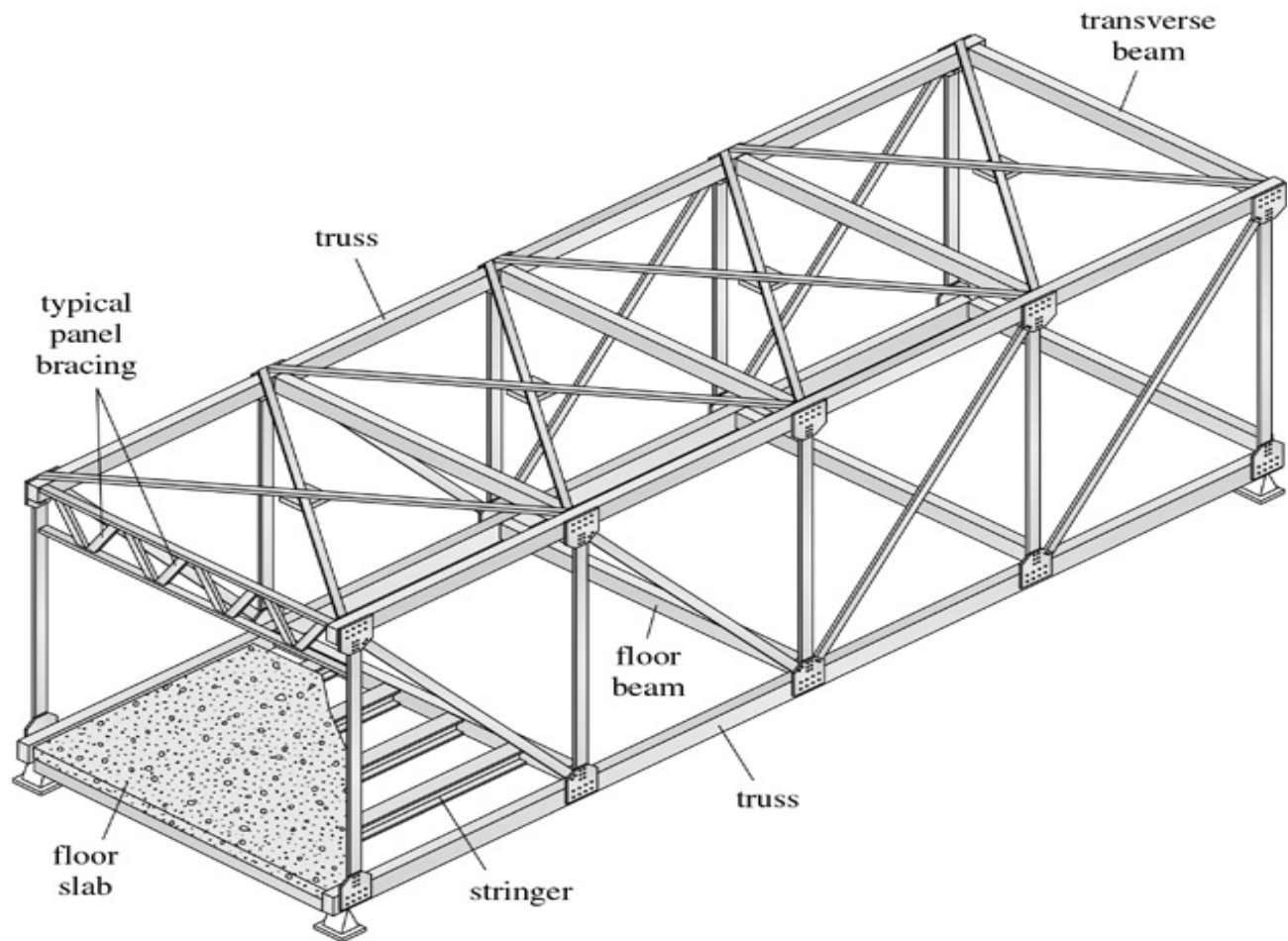


(a)

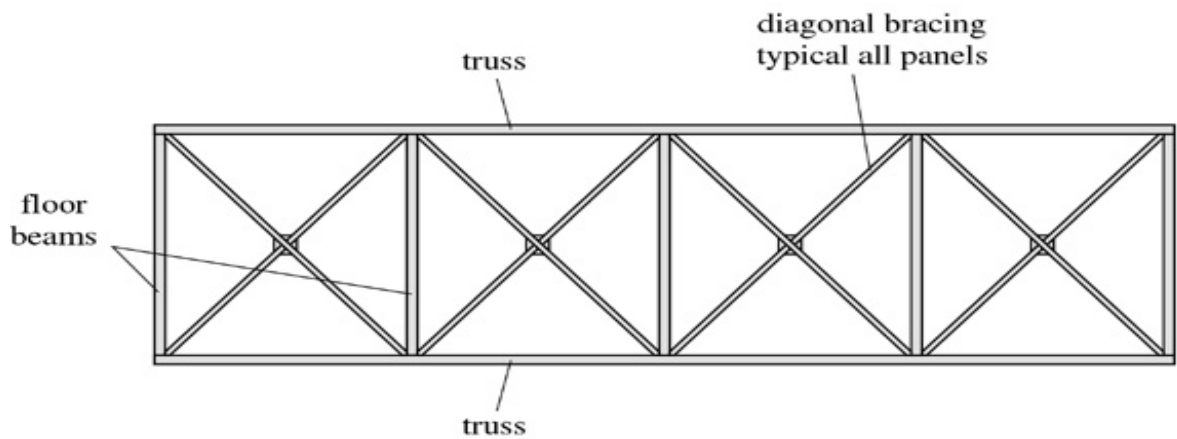


(b)

Truss: Mimic Beam Behavior

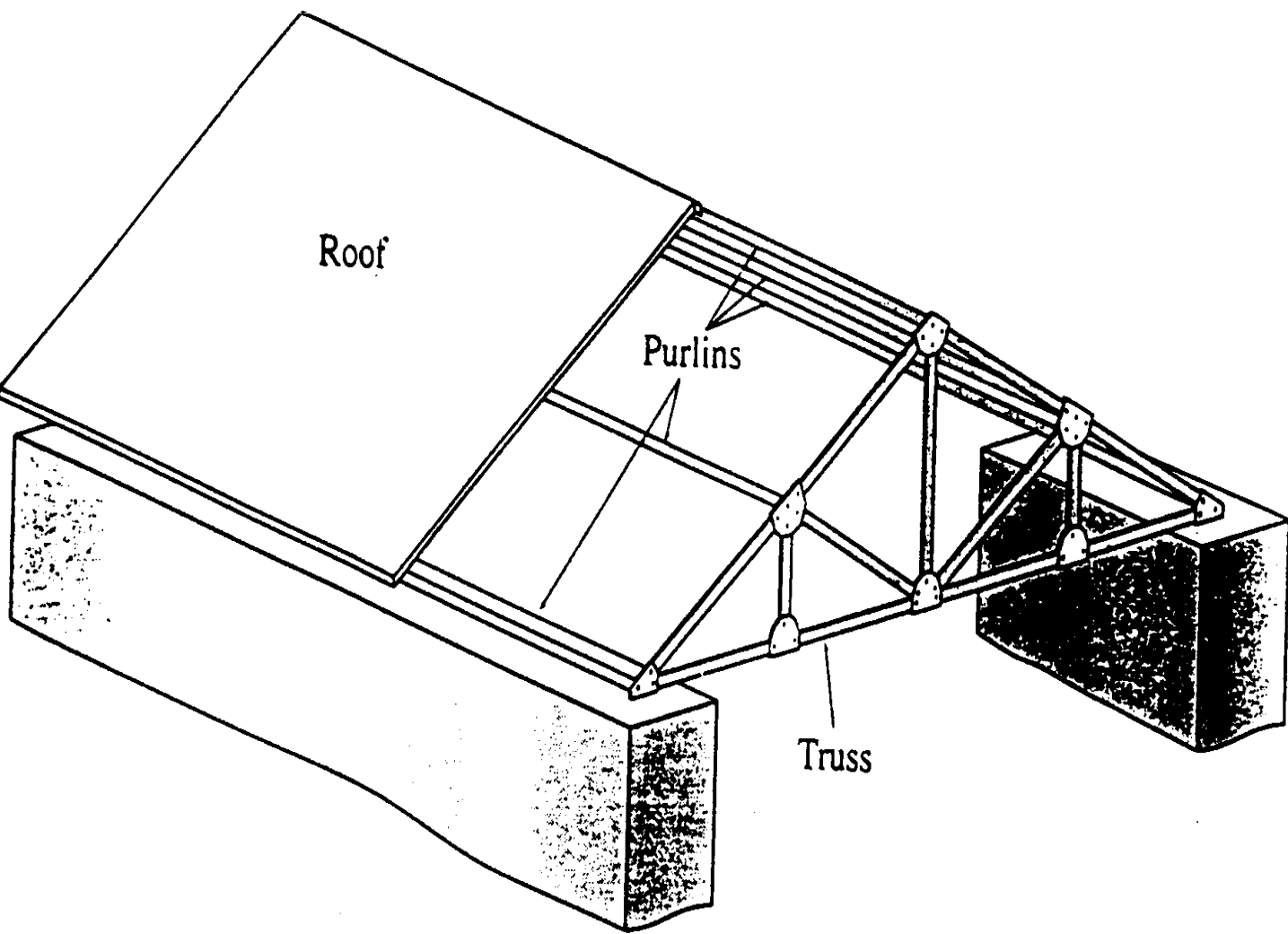


(a)

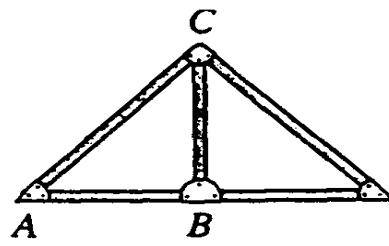


(b)

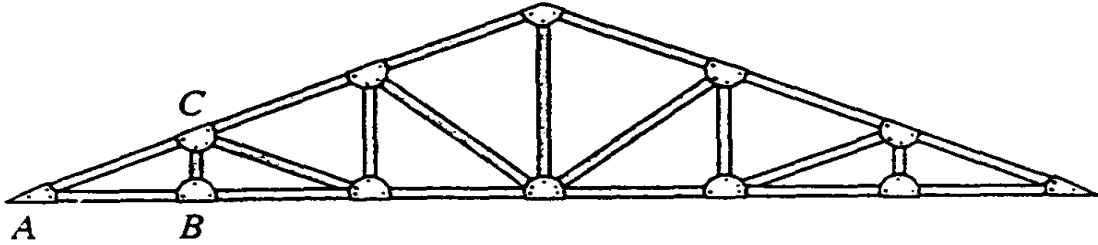
Bridge Truss Details



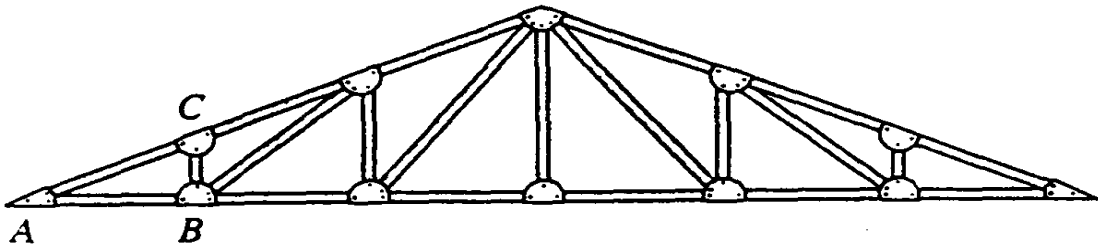
Framing of a Roof Supported Truss



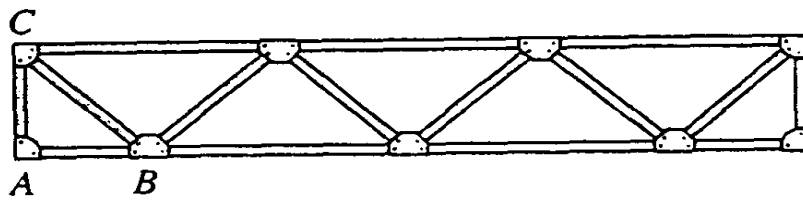
King post truss



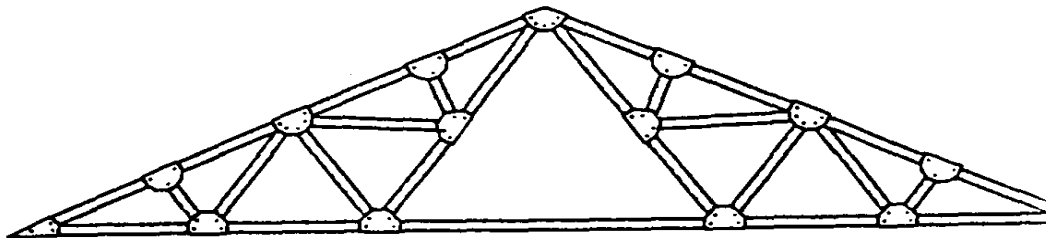
Howe truss



Pratt truss

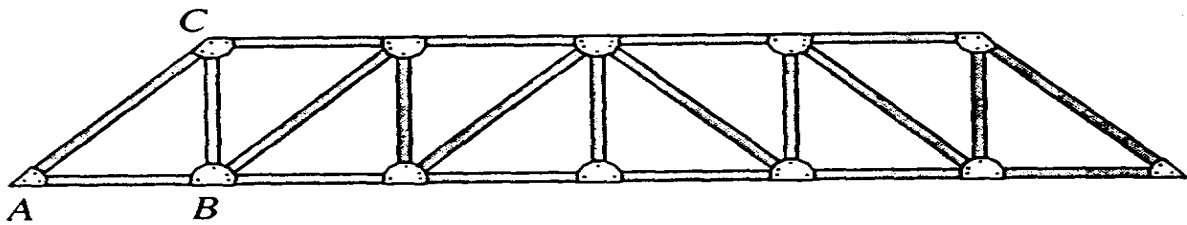


Warren truss

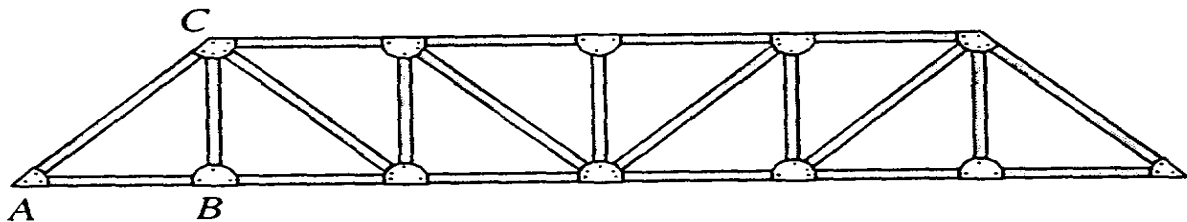


Fink truss

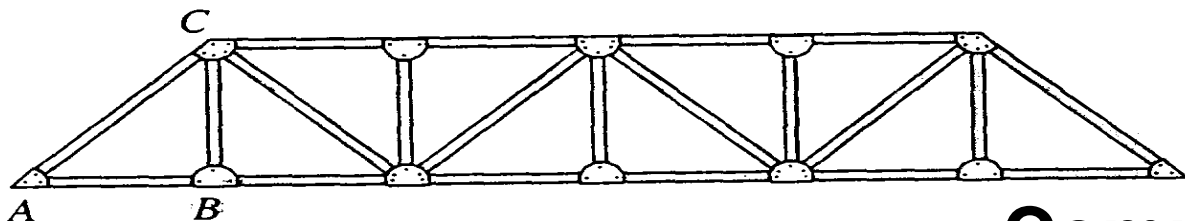
Common Roof Trusses



Howe truss

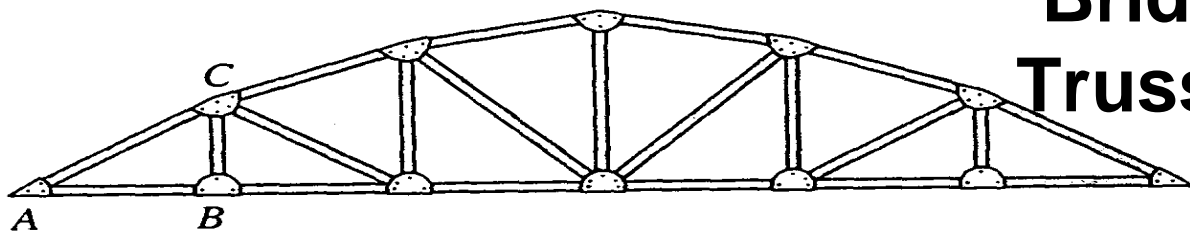


Pratt truss

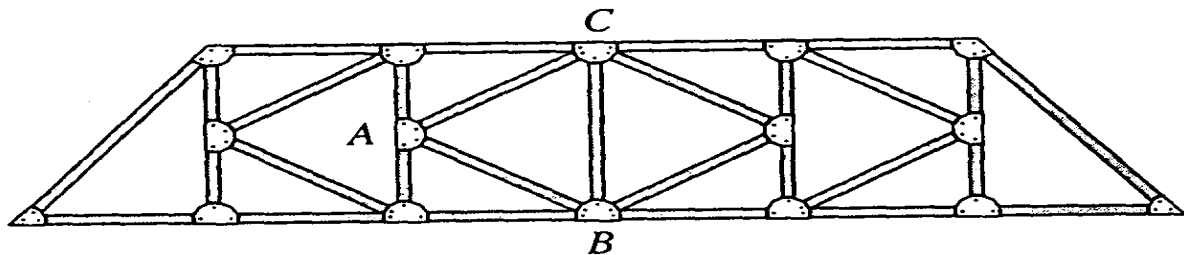


Warren truss

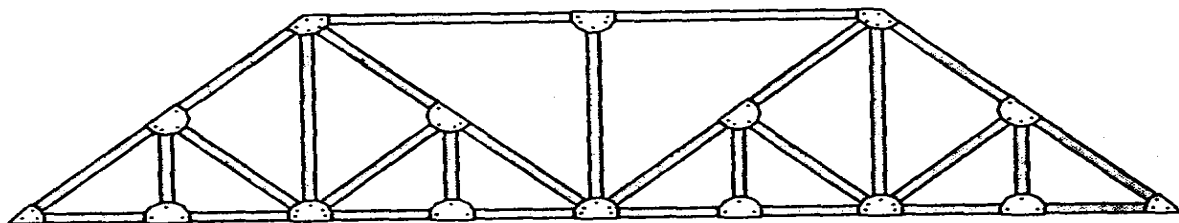
Common Bridge Trusses



Parker truss



K truss



Baltimore truss

Buckling Calculations

$$P_{cr} = \frac{\pi^2 EI_{weak}}{(kL)^2}$$

= buckling force

k = effective length factor

k = 1 for an ideal truss member

Types of Trusses

Basic Truss Element

≡ three member triangular truss

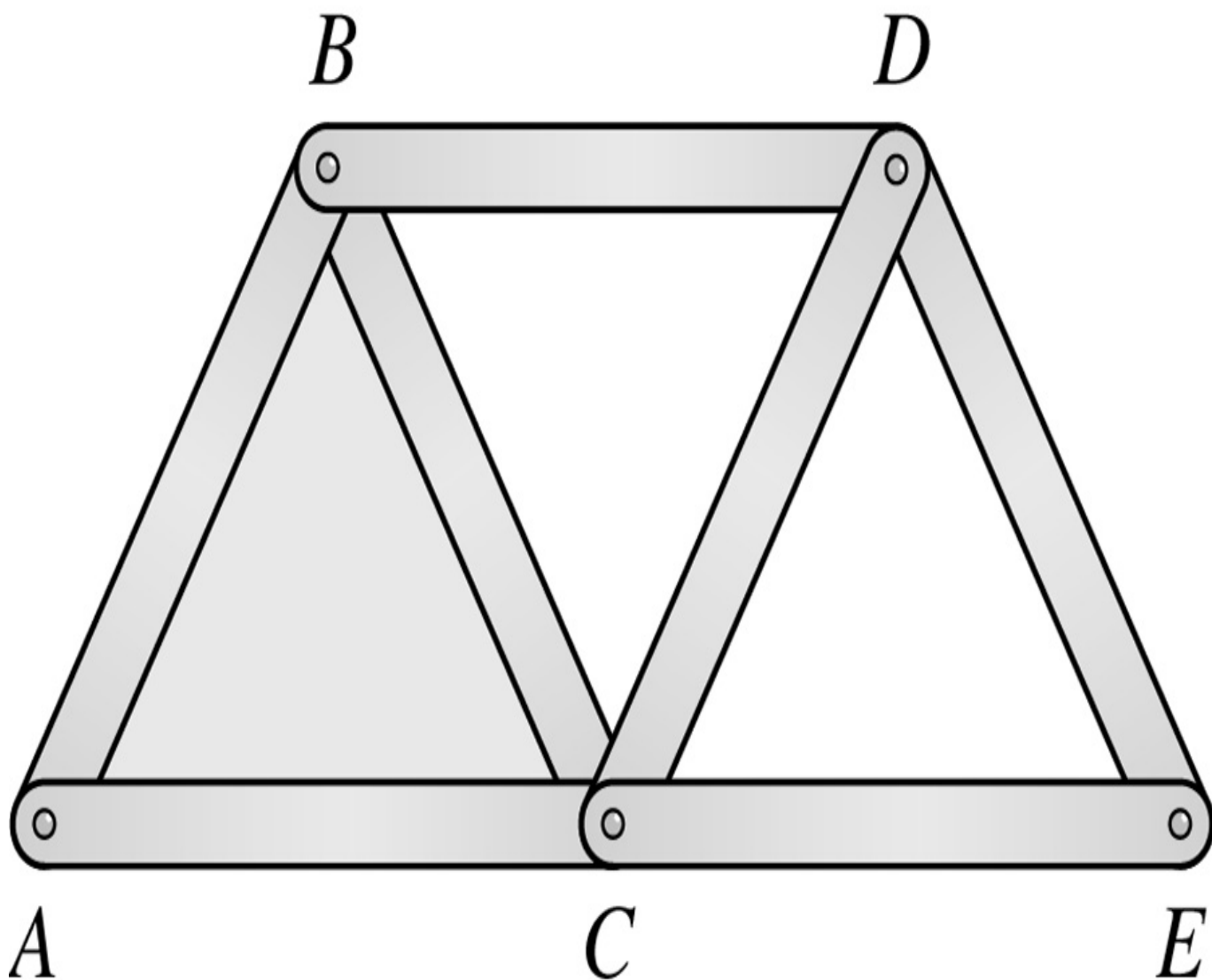
Simple Trusses – composed of basic truss elements

$$m = 3 + 2(j - 3) = 2j - 3$$

for a simple truss

m ≡ total number of members

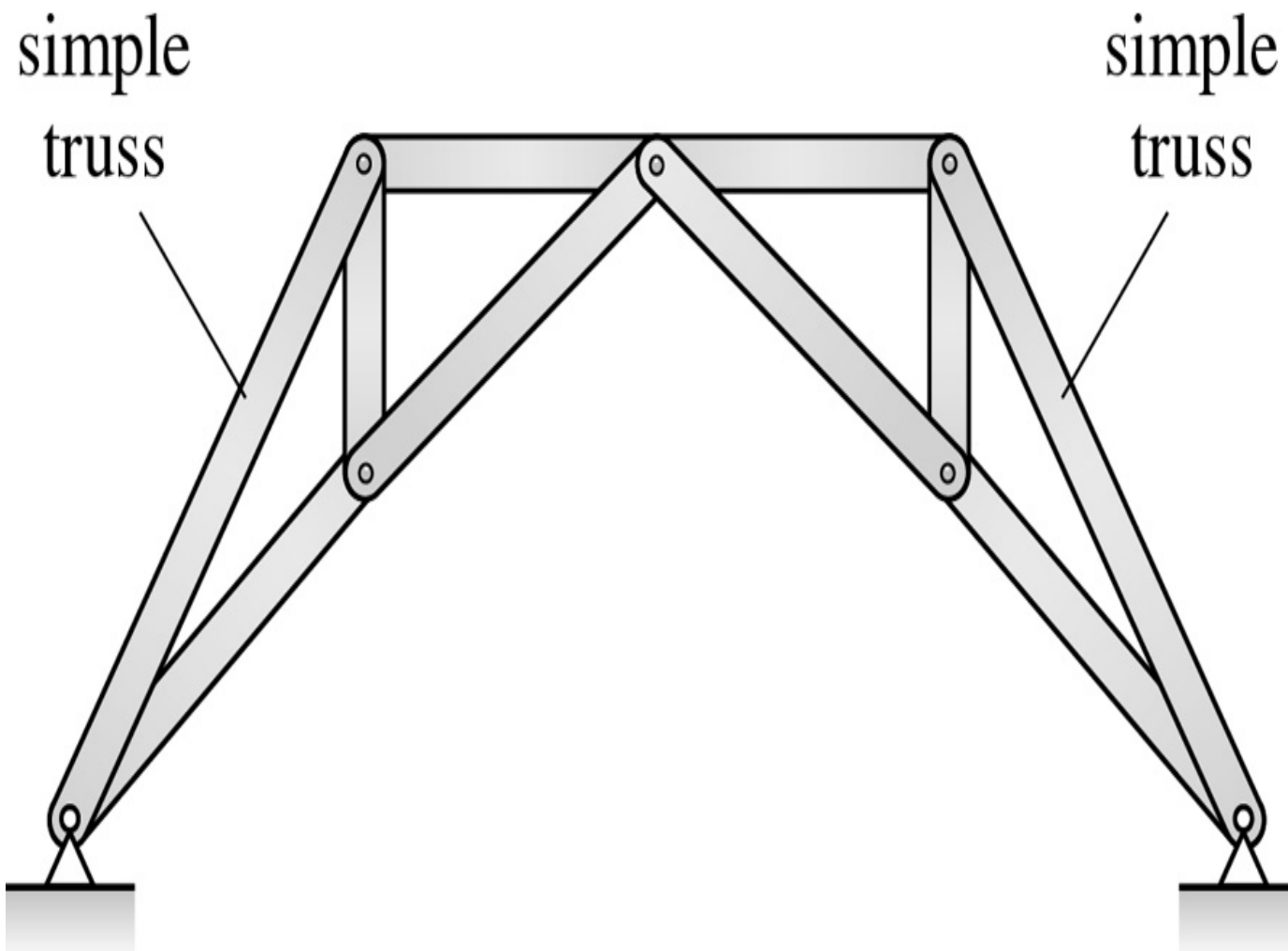
j ≡ total number of joints



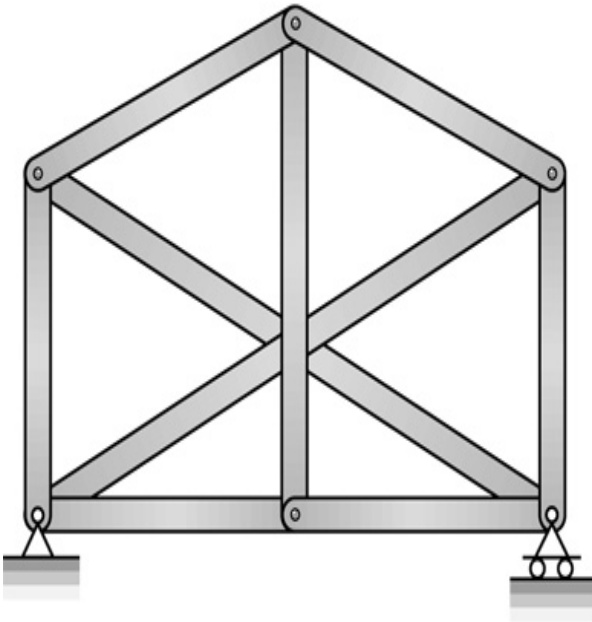
Simple Truss

Compound Trusses –

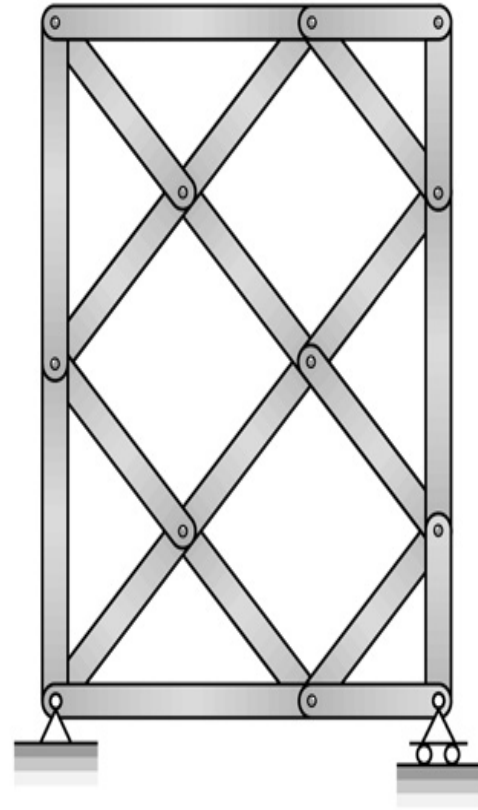
constructed by connecting two or more simple trusses to form a single rigid body



Complex Trusses – truss that is neither simple nor compound



(a)



(b)

Analysis of Trusses

The analysis of trusses is usually based on the following simplifying assumptions:

- The centroidal axis of each member coincides with the line connecting the centers of the adjacent members and the members only carry axial force.
- All members are connected only at their ends by frictionless hinges in plane trusses.
- All loads and support reactions are applied only at the joints.

The reason for making these assumptions is to obtain an ideal truss, i.e., a truss whose members are subjected only to axial forces.

Primary Forces \equiv member axial forces determined from the analysis of an ideal truss

Secondary Forces \equiv deviations from the idealized forces, i.e., shear and bending forces in a truss member.

Our focus will be on primary forces. If large secondary forces are anticipated, the truss should be analyzed as a frame.

Method of Joints

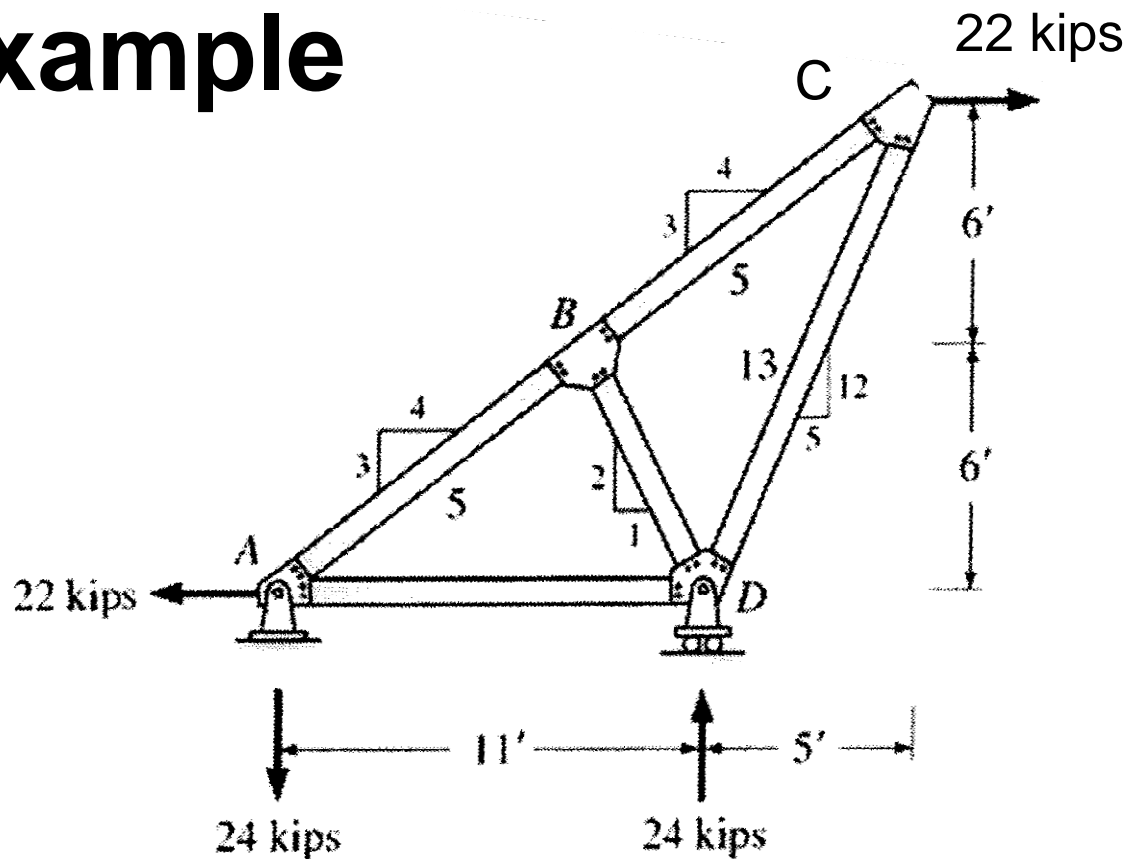
Method of Joints - the axial forces in the members of a statically determinate truss are determined by considering the equilibrium of its joints.

Tensile (T) axial member force is indicated on the joint by an arrow pulling away from the joint.

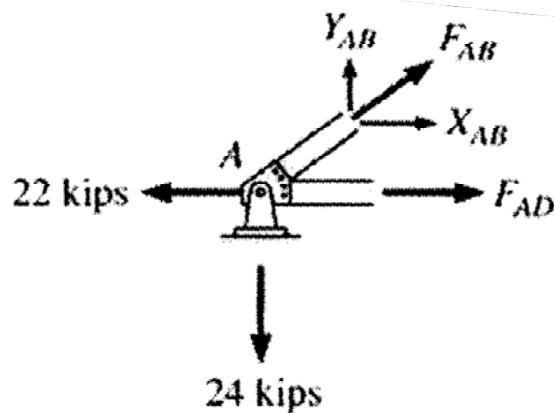
Compressive (C) axial member force is indicated by an arrow pushing toward the joint.

Method of Joints

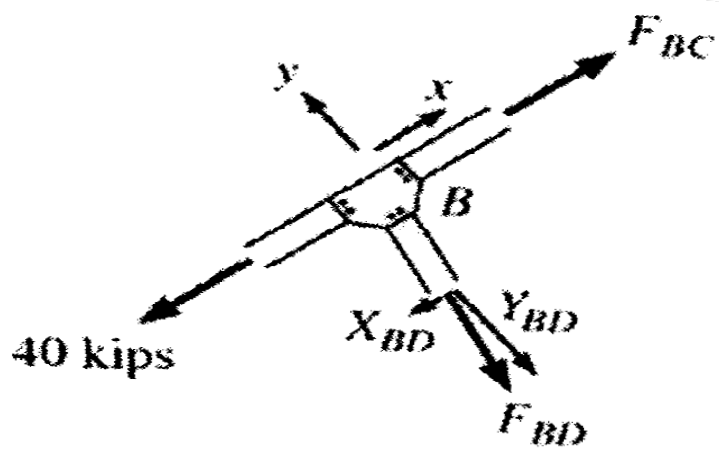
Example



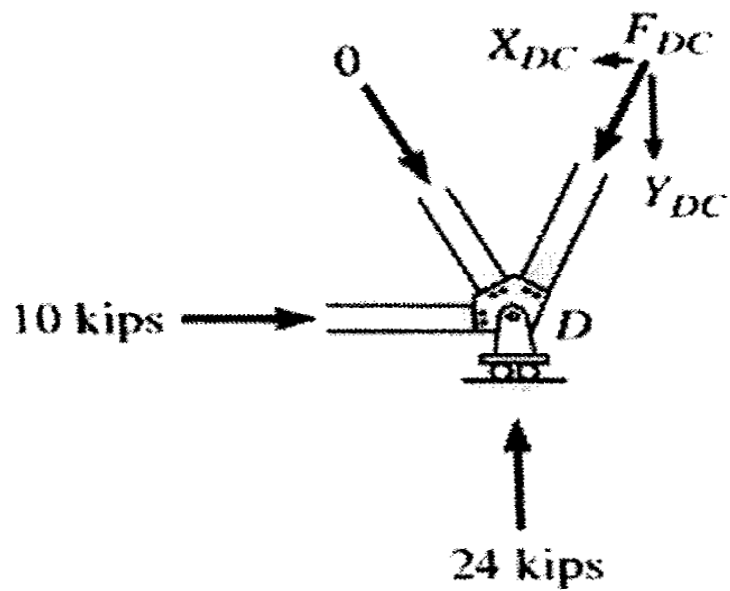
(a)



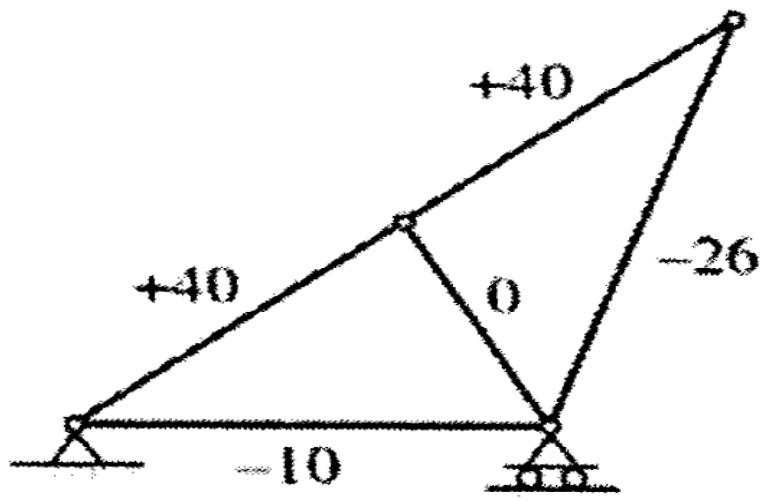
(b)



(c)



(d)

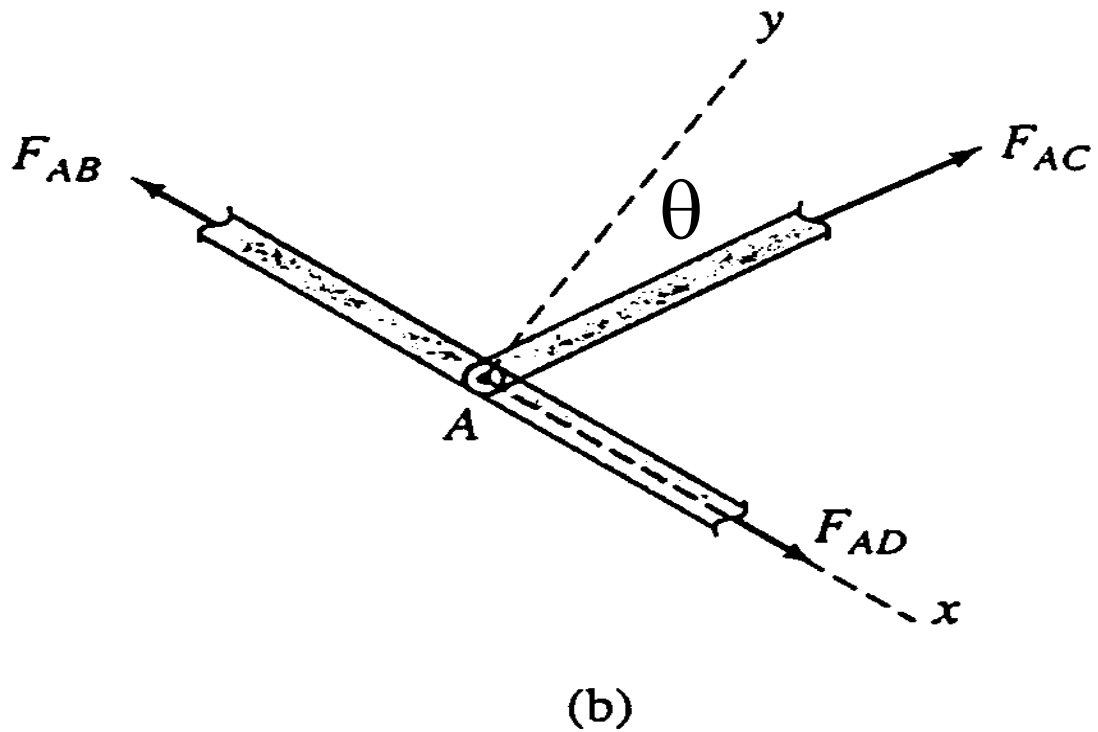
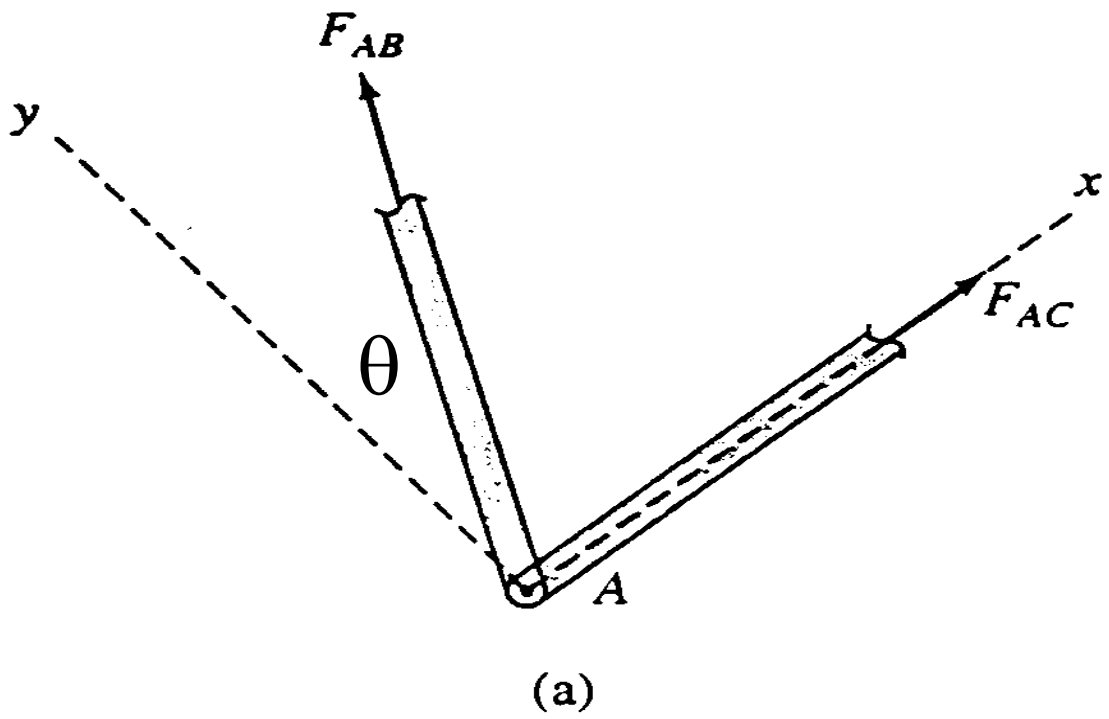


(e)

Truss Solution

Zero Force Members:

- (a) If only two noncollinear members are connected to a joint that has no external loads or reactions applied to it, then the force in both members is zero.
- (b) If three members, two of which are collinear, are connected to a joint that has no external loads or reactions applied to it, then the force in the member that is not collinear is zero.



Zero Force Members

Zero Member Force Calculations

Figure (a):

$$\sum F_y = 0 = F_{AB} \cos \theta$$

$$\therefore F_{AB} = 0$$

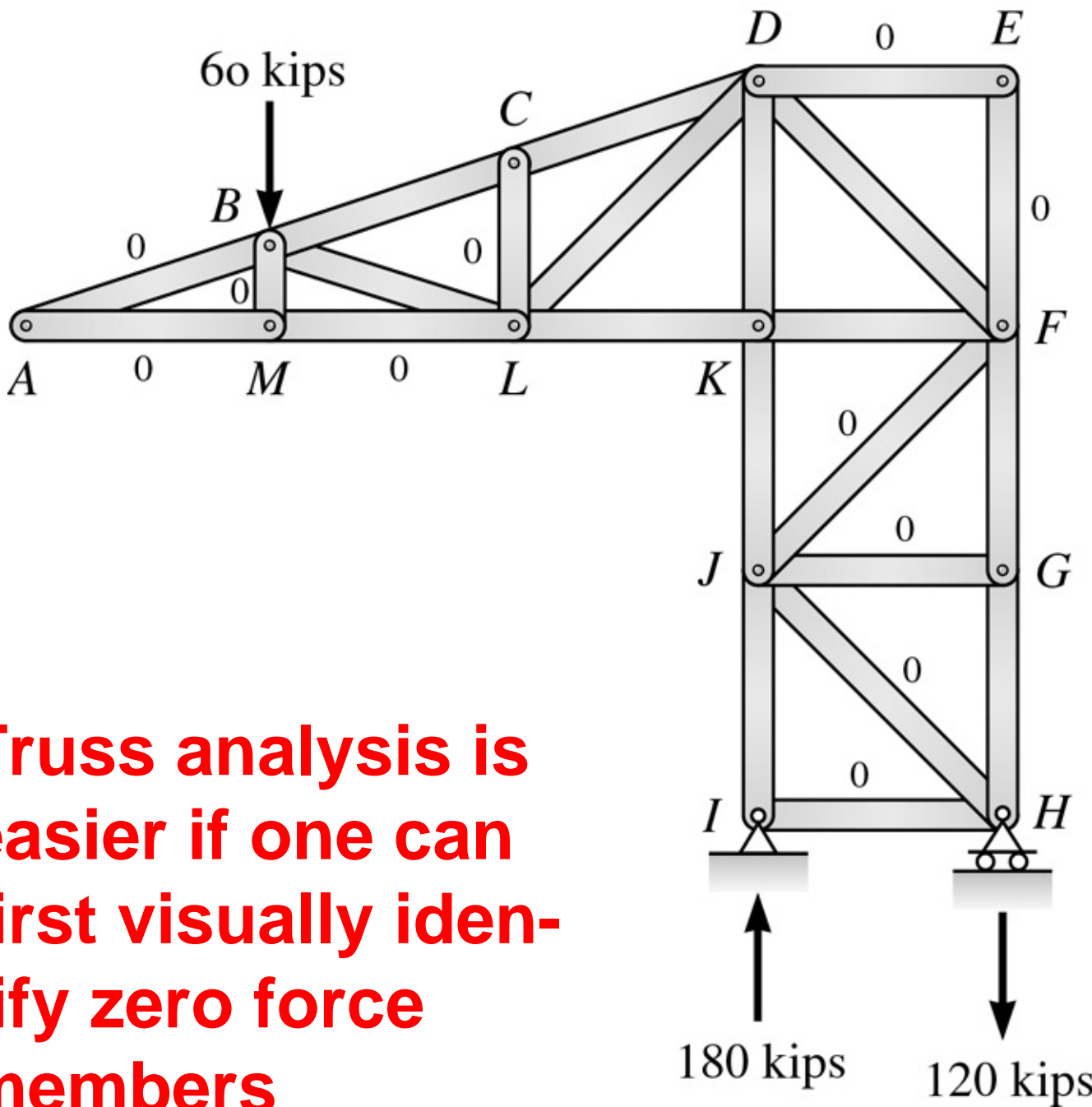
$$\sum F_x = 0 = F_{AC} + \cancel{F_{AB} \sin \theta} \quad \text{0}$$

$$\therefore F_{AC} = 0$$

Figure (b):

$$\sum F_y = 0 = F_{AC} \cos \theta$$

$$\therefore F_{AC} = 0$$

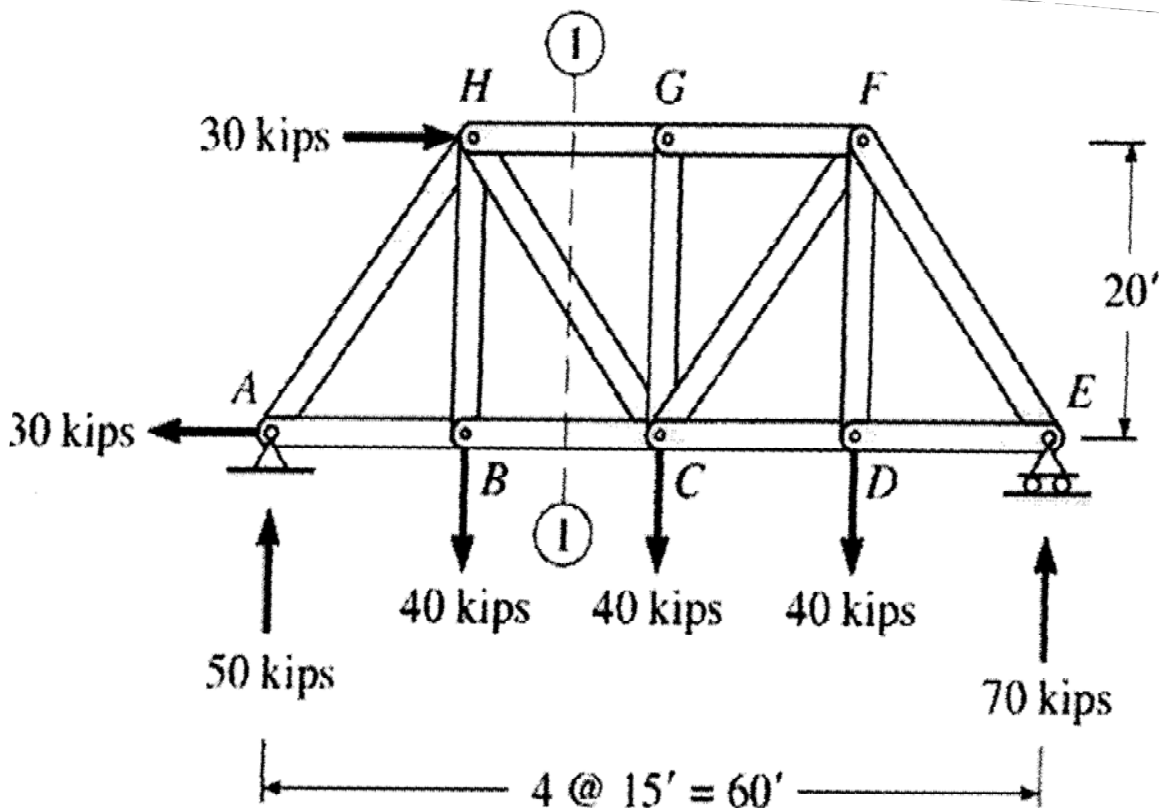


Method of Sections

The method of sections enables one to determine forces in specific truss members directly.

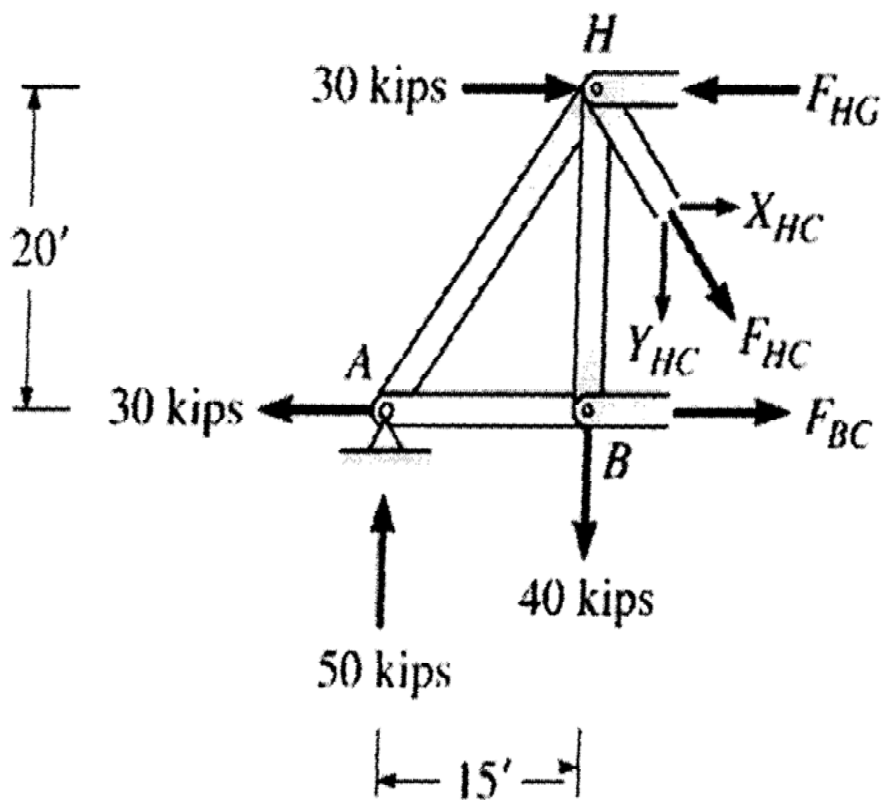
Method of Sections \equiv involves cutting the truss into two portions (free body diagrams, FBD) by passing an imaginary section through the members whose forces are desired. Desired member forces are determined by considering equilibrium of one of the two FBD of the truss.

Method of sections can be used to determine three unknown member forces per FBD since all three equilibrium equations can be used.



(a)

Method of Sections Example



(b)

$$F_{BC} = \underline{\hspace{2cm}}$$

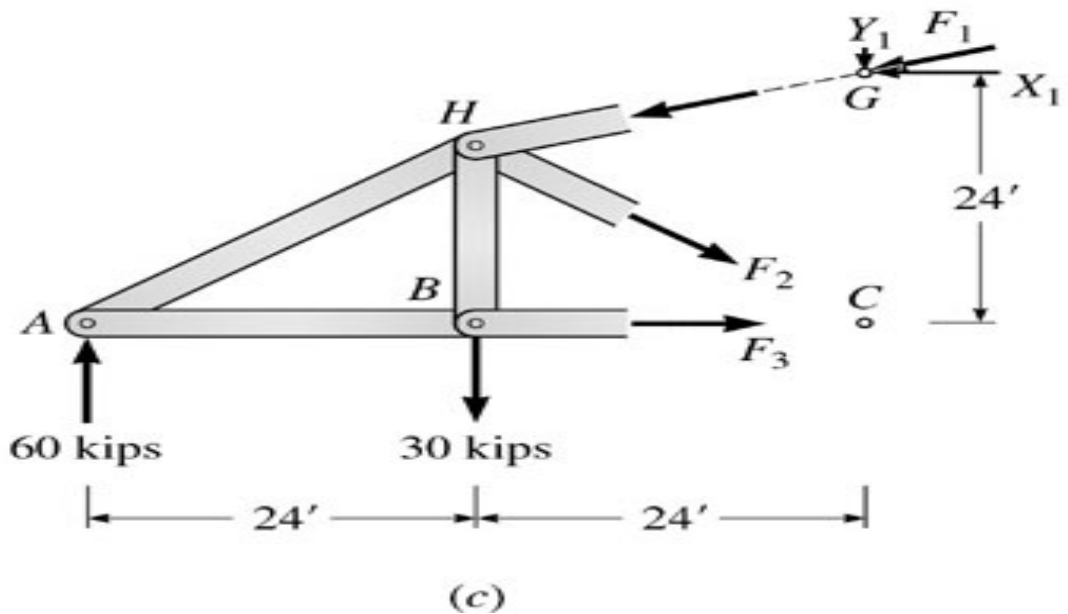
$$F_{HG} = \underline{\hspace{2cm}}$$

$$F_{HC} = \underline{\hspace{2cm}}$$

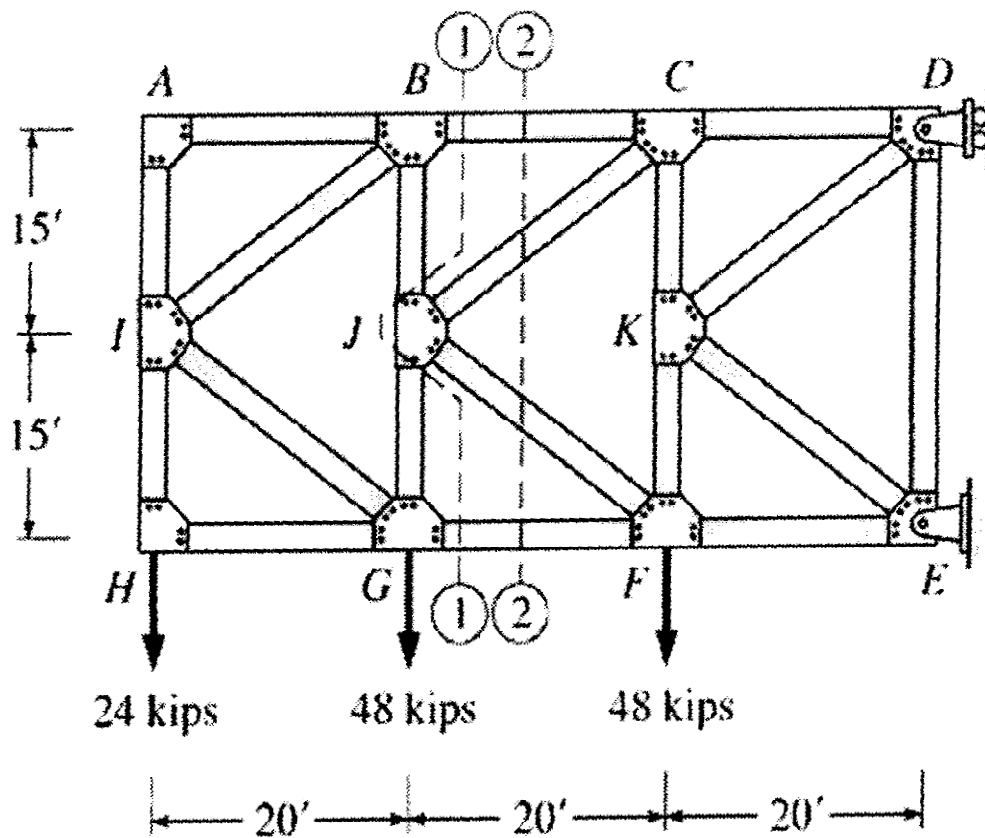
[illegible]

The diagram shows a truss structure with a horizontal bottom chord and a vertical member. The bottom chord has a pin support at point A and a roller support at point B. A horizontal member extends from B to point C. A vertical member connects point B to point H. A diagonal member connects point A to point H. A horizontal member extends from point H to the right, where a force F_1 is applied. A diagonal member connects point H to point C, where a force F_2 is applied. A horizontal force F_3 is applied at point C. A dashed line extends from point A through point H to a point 'a' on the left. The horizontal distance from A to B is x , from B to H is 24', and from H to C is 24'. Upward and downward arrows at A and B are labeled 60 kips and 30 kips, respectively. At point C, a coordinate system is shown with X_2 horizontal and Y_2 vertical, and a force F_2 is shown acting at an angle.

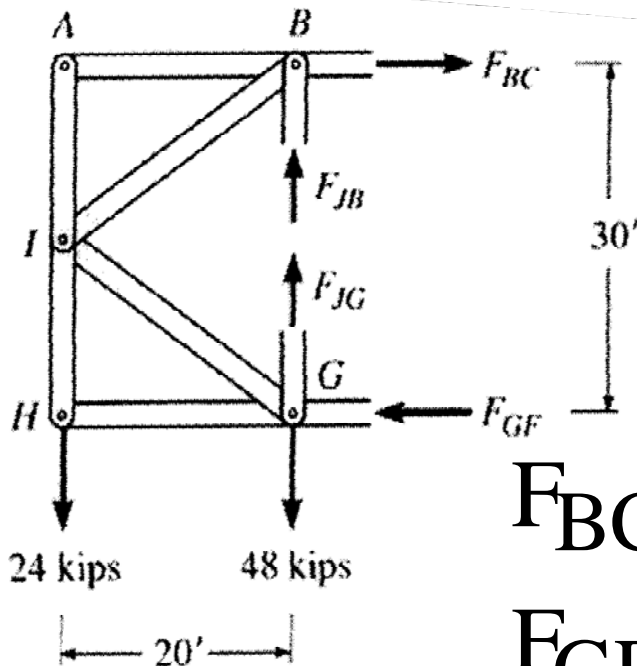
25



Transmissibility principle of statics states that a force can be applied at any point on its line of action without a change in the external effects



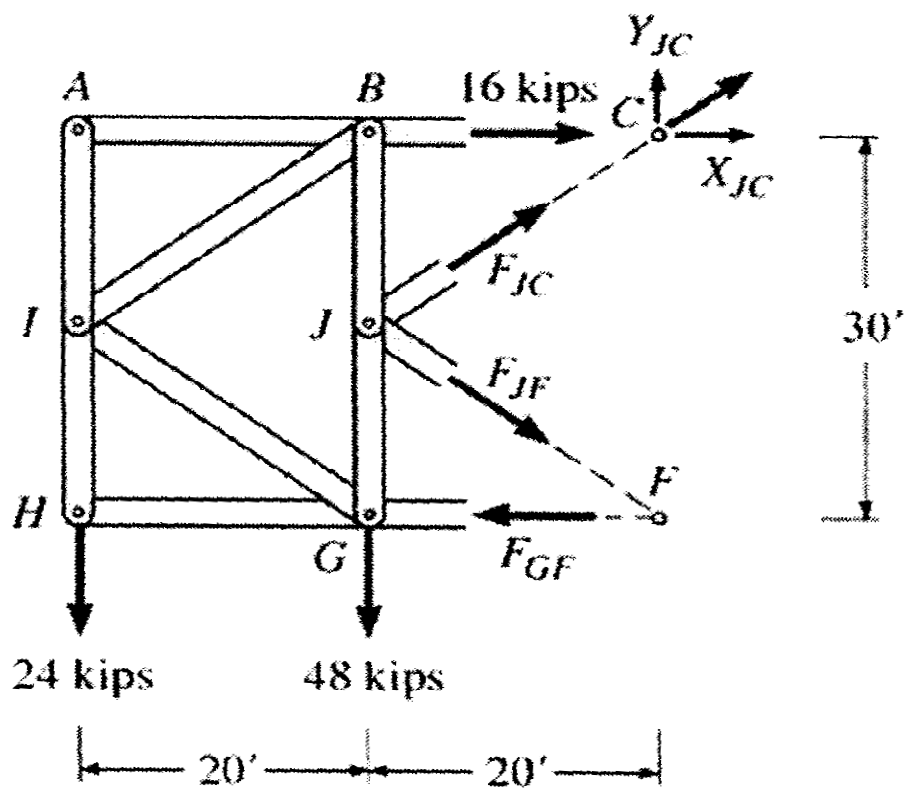
(a)



$$F_{BC} = \underline{\hspace{2cm}}$$

$$F_{GF} = \underline{\hspace{2cm}}$$

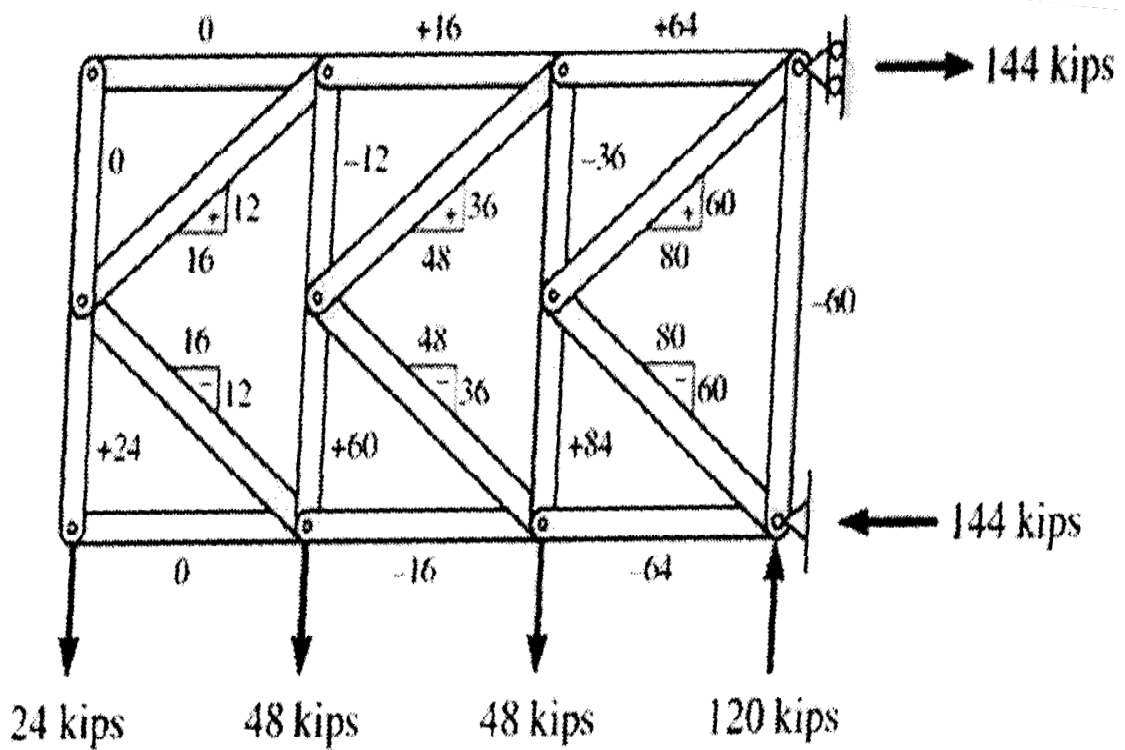
(b)



(c)

$$F_{JC} = \underline{\hspace{2cm}}$$

$$F_{JF} = \underline{\hspace{2cm}}$$



(d)

K-Truss Solution

Determinacy and Stability

Internal Stability \equiv number and arrangement of members is such that the truss does not change its shape when detached from the supports.

External Instability \equiv instability due to insufficient number or arrangement of external supports.

Internal Stability

$$m < 2j - 3$$

\Rightarrow truss is internally unstable

$$m \geq 2j - 3$$

\Rightarrow truss is internally stable provided it is geometrically stable

m \equiv total number of members

j \equiv total number of joints

Geometric stability in the second condition requires that the members be properly arranged.

Statically Determinate Truss \equiv
if all the forces in all its members
as well as all the external reactions
can be determined by
using the equations of
equilibrium.

Statically Indeterminate Truss
 \equiv if all the forces in all its members
as well as all the external
reactions cannot be determined
by using the equations of equilibrium.

External Indeterminacy \equiv
excess number of support
reactions

Internal Indeterminacy \equiv excess number of members

Redundants \equiv excess members or reactions

Number of redundants defines the degree of static indeterminacy **I**

Summary

$$m + R < 2j$$

\Rightarrow statically unstable truss

$$m + R = 2j$$

\Rightarrow statically determinate truss

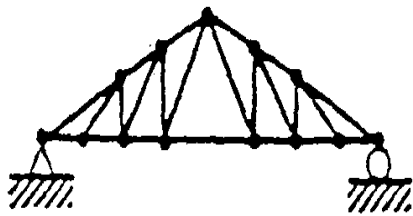
$$m + R \geq 2j$$

\Rightarrow statically indeterminate truss

The first condition is always true.

But, the **last two conditions are true if and only if the truss is geometrically stable.**

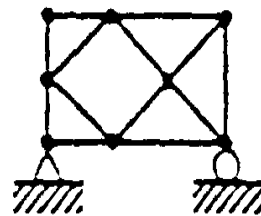
The analysis of unstable trusses will always lead to inconsistent, indeterminant, or infinite results.



$$m + r = 2j$$

$$23 + 3 = 26$$

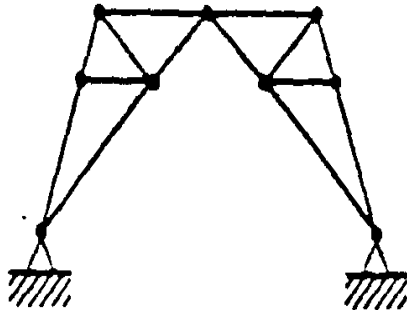
Determinate



$$m + r = 2j$$

$$13 + 3 = 16$$

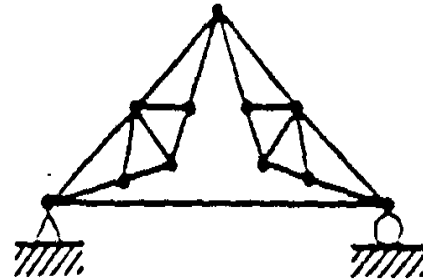
Determinate



$$m + r = 2j$$

$$14 + 4 = 18$$

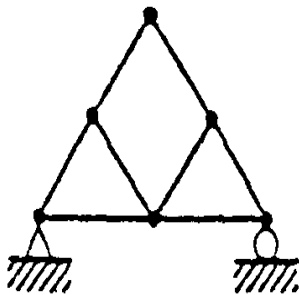
Determinate



$$m + r = 2j$$

$$19 + 3 = 22$$

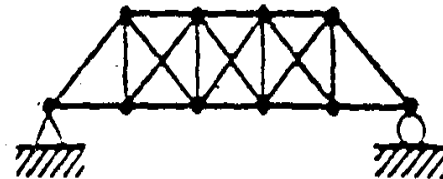
Determinate



$$m + r < 2j$$

$$8 + 3 < 12$$

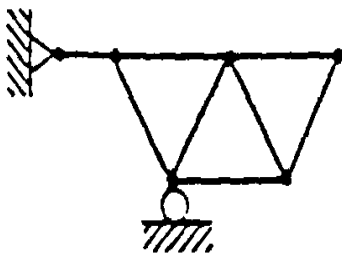
Unstable



$$m + r > 2j$$

$$20 + 3 > 26$$

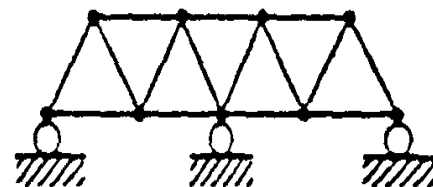
3 Redundants



$$m + r < 2j$$

$$8 + 3 < 12$$

Unstable

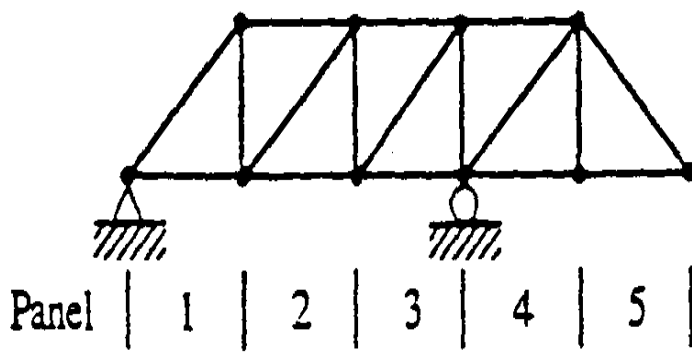


$$m + r = 2j$$

$$15 + 3 = 18$$

Unstable

Truss Determinacy Calculations



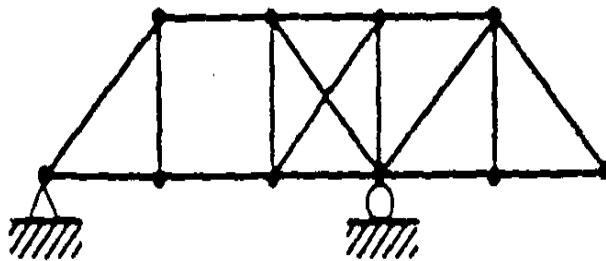
(a)

$$m = 17$$

$$r = 3$$

$$j = 10$$

$m + r = 2j$
 Statically
 determinate
 and stable



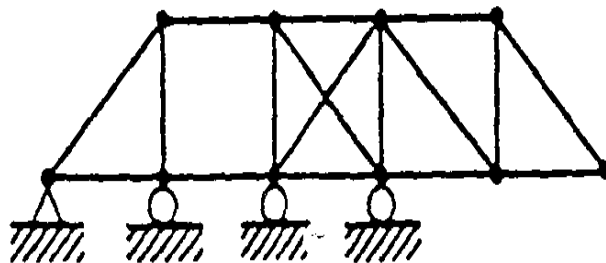
(b)

$$m = 17$$

$$r = 3$$

$$j = 10$$

$m + r = 2j$
 Unstable



(c)

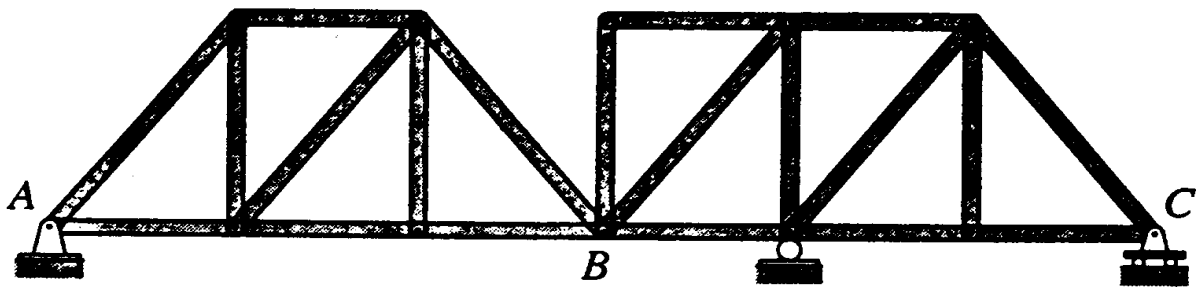
$$m = 19$$

$$r = 5$$

$$j = 10$$

$m + r > 2j$
 Stable
 2 redundants

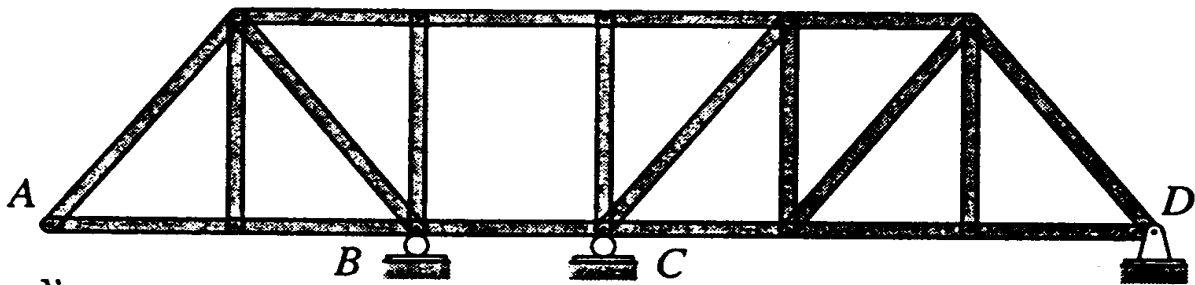
Truss Determinacy Calculations



One equation of condition:

$$\Sigma M_B^{AB} = 0 \quad \text{or} \quad \Sigma M_B^{BC} = 0$$

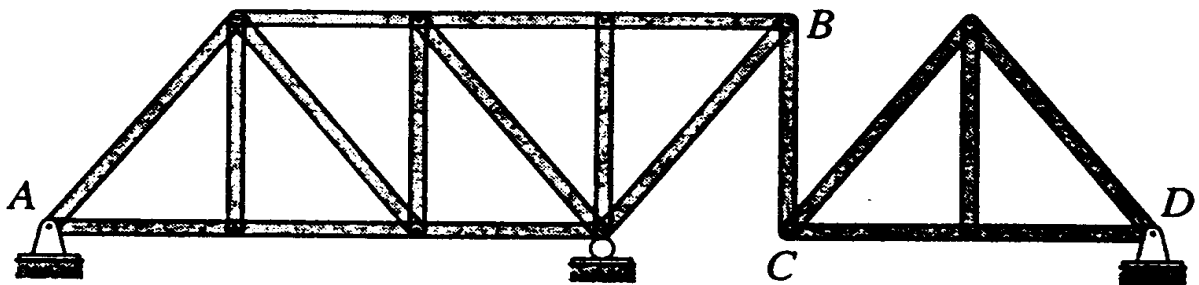
(a)



One equation of condition:

$$\Sigma F_y^{AB} = 0 \quad \text{or} \quad \Sigma F_y^{CD} = 0$$

(b)



Two equations of condition:

$$\Sigma F_x^{AB} = 0 \quad \text{or} \quad \Sigma F_x^{CD} = 0$$

$$\Sigma M_B^{AB} = 0 \quad \text{or} \quad \Sigma M_C^{CD} = 0$$

(c)

Equations of Condition: Plane Trusses